

Implicit
DifferentiationChapter: Differential Calculus · Level ★★★ ·
Time: 30 min

SCORE

___ / 20

Name _____ Class _____ Date _____

AFTER THIS WORKSHEET YOU CAN

- ✓ Differentiate equations in which y is not isolated.
- ✓ Treat y as a function of x and apply the chain rule to y -terms.
- ✓ Solve the resulting equation for dy/dx .
- ✓ Find slopes of tangents to curves such as circles.



Section A · Concept Check

• BEGINNER

$4 \times 1 = 4$

- For $x^2 + y^2 = 49$, $dy/dx = ?$
☐ A. $-x/y$ ☐ B. x/y ☐ C. $-y/x$ ☐ D. y/x
- Differentiating y^2 with respect to x gives:
☐ A. $2y$ ☐ B. $2y \cdot dy/dx$ ☐ C. 2 ☐ D. y^2
- For $xy = 20$, $dy/dx = ?$
☐ A. y/x ☐ B. $-y/x$ ☐ C. $-x/y$ ☐ D. 1
- Implicit differentiation is needed when:
☐ A. y is isolated ☐ B. y cannot easily be isolated
☐ C. there is no y ☐ D. f is linear



Section B · Problem Solving

• INTERMEDIATE

$2 + 3 \times 3 = 11$

- $d/dx[y^2] =$ _____
- For $x^2 + y^2 = 49$, $dy/dx =$ _____
- Find dy/dx for $x^2 + y^2 = 49$.

- Find dy/dx for $x^3 + y^3 = 8$.

- Find dy/dx for $xy = 20$.



Section C · Challenge

• CHALLENGE

5

- Find dy/dx for $x^2 - y^2 = 16$.

Reflection — the most useful thing I learned: _____

A ___/4 B ___/11 C ___/5 Total ___/20

Teacher's Signature _____

Parent's Signature _____

ANSWER KEY — FOLD OR CUT BEFORE HANDING OUT

1-A 2-B 3-B 4-B | 5 $2y \cdot dy/dx$ 6 $-x/y$ 7 $= -x/y$ 8 $= -x^2/y^2$ 9 $= -y/x$ | 10 $= x/y$